



Benchmark Example No. 6

Design of a Rectangular CS for Shear Force

SOFiSTiK | 2023

VERiFiCATION
DCE-EN6 Design of a Rectangular CS for Shear Force

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The manual and the program have been thoroughly checked for errors. However, SOFiSTiK does not claim that either one is completely error free. Errors and omissions are corrected as soon as they are detected.

The user of the program is solely responsible for the applications. We strongly encourage the user to test the correctness of all calculations at least by random sampling.

Front Cover

Volkstheater, Munich Photo: Florian Schreiber

Overview

Design Code Family(s): EN, DIN
Design Code(s): DIN EN 1992-1-1, EN 1992-1-1
Module(s): AQB
Input file(s): [rectangular_shear.dat](#)

1 Problem Description

The problem consists of a rectangular section, symmetrically reinforced for bending, as shown in Fig. 1. The cross-section is designed for shear force V_{Ed} and the required shear reinforcement is determined.

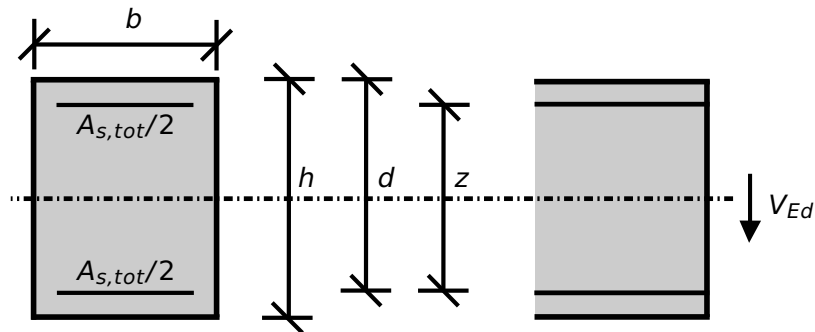


Figure 1: Problem Description

2 Reference Solution

This example is concerned with the design of sections for ULS, subject to shear force. The content of this problem is covered by the following parts of DIN EN 1992-1-1:2004 [1] [2]:

- Design stress-strain curves for concrete and reinforcement (Section 3.1.7, 3.2.7)
- Guidelines for shear design (Section 6.2)
- Reinforcement (Section 9.2.2)

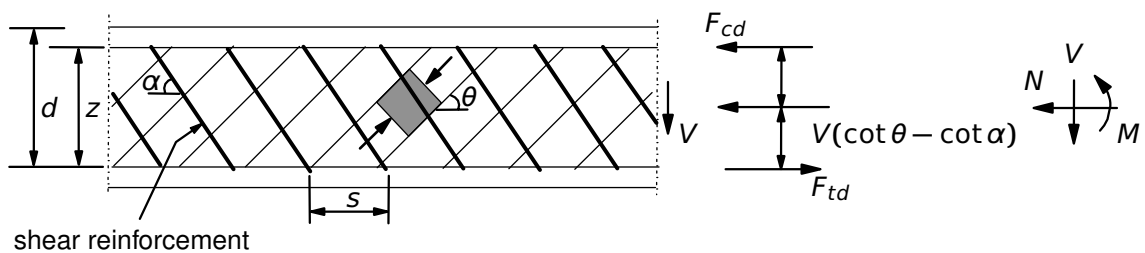


Figure 2: Shear Reinforced Members

The design stress-strain diagram for reinforcing steel considered in this example, consists of an inclined top branch, as presented in Fig. 3 and as defined in DIN EN 1992-1-1:2004 [1] (Section 3.2.7).

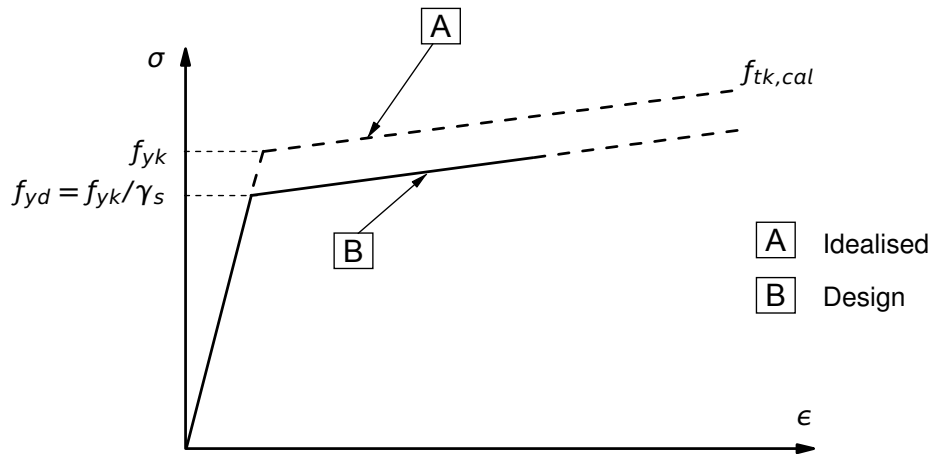


Figure 3: Idealised and Design Stress-Strain Diagram for Reinforcing Steel

3 Model and Results

The rectangular section, with properties as defined in Table 1, is to be designed, with respect to DIN EN 1992-1-1:2004 (German National Annex) [1], [2], under shear force of 343.25 kN. The reference calculation steps are presented below and the results are given in Table 2. Then, the same section is designed with respect to EN 1992-1-1:2004 [3]. The same angle $\theta (= 1.60)$ is chosen, as calculated with respect to DIN EN 1992-1-1:2004, in order to compare the results. If no θ value is input, then the calculation starts with the upper limit $\cot \theta = 2.5$ and through an optimization process the right angle is selected. In this case, the reinforcement is determined with $\cot \theta = 2.5$, giving a shear reinforcement of $7.80 \text{ cm}^2/\text{m}$. Also in order to demonstrate that the correct value of $V_{Rd,max} = 734.4 \text{ kN}$ (reference value) with respect to DIN EN 1992-1-1:2004 is calculated in SOFiSTiK, we input a design shear force of 734.3 delivering a shear reinforcement, but when a value of 734.4 is input then AQB gives the warning of 'no shear design possible' showing that the maximum shear resistance is exceeded.

Table 1: Model Properties

Material Properties	Geometric Properties	Loading
C 30/37	$h = 50.0 \text{ cm}$	$V_{Ed} = 343.25 \text{ kN}$
B 500A	$b = 30 \text{ cm}$ $d = 45.0 \text{ cm}$ $A_{s,tot} = 38.67 \text{ cm}^2$	

Table 2: Results

$A_{s,tot} [\text{cm}^2/\text{m}]$	Design Code	SOF.	Ref.
	DIN EN [1]	12.84	12.84
	EN [3]	12.18	12.18

4 Design Process¹

Material:

Concrete: $\gamma_c = 1.50$

(NDP) 2.4.2.4: (1), Tab. 2.1DE: Partial factors for materials

Steel: $\gamma_s = 1.15$

$f_{ck} = 30 \text{ MPa}$

$f_{cd} = a_{cc} \cdot f_{ck} / \gamma_c = 0.85 \cdot 30 / 1.5 = 17.0 \text{ MPa}$

Tab. 3.1: Strength for concrete

3.1.6: (1)P, Eq. (3.15): $a_{cc} = 0.85$ considering long term effects

3.2.2: (3)P: yield strength $f_{yk} = 500 \text{ MPa}$

3.2.7: (2), Fig. 3.8

$f_{yk} = 500 \text{ MPa}$

$f_{yd} = f_{yk} / \gamma_s = 500 / 1.15 = 434.78 \text{ MPa}$

Design Load: $V_{Ed} = 343.25 \text{ kN}$

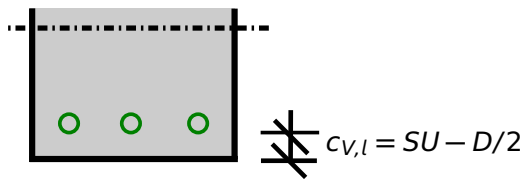
Design with respect to DIN EN 1992-1-1:2004 (NA) [1] [2]:²

$z = \max \{ d - c_{v,l} - 30 \text{ mm}; d - 2 c_{v,l} \}$

(NDP) 6.2.3 (1): Inner lever arm z

$c_{v,l} = SU - D/2 = 50 - 28/2 = 36 \text{ mm}$

$z = \max \{ 450 - 36 - 30 \text{ mm}; 450 - 2 \cdot 36 \}$



$z = \max \{ 384; 378 \} = 384 \text{ mm}$

$1.0 \leq \cot \theta \leq \frac{1.2 + 1.4 \sigma_{cd} / f_{cd}}{1 - V_{Rd,cc} / V_{Ed}} \leq 3.0$

(NDP) 6.2.3 (2): Eq. 6.7aDE

$V_{Rd,cc} = c \cdot 0.48 \cdot f_{ck}^{1/3} \cdot \left(1 - 1.2 \frac{\sigma_{cd}}{f_{cd}} \right) \cdot b_w \cdot z$

(NDP) Eq. 6.2.3 (2): 6.7bDE
 $c = 0.5$

$V_{Rd,cc} = 0.5 \cdot 0.48 \cdot 30^{1/3} \cdot (1 - 0) \cdot 0.3 \cdot 0.384$

(NDP) 6.2.3 (2): $\sigma_{cd} = N_{Ed} / A_c$

$V_{Rd,cc} = 0.08591 \text{ MN} = 85.91 \text{ kN}$

$\cot \theta = \frac{1.2 + 0}{1 - 85.91 / 343.25} = 1.60$

(NDP) 6.2.3 (2): The angle θ should be limited by Eq. 6.7DE

$A_{sw,requ} / s = V_{Ed} / (f_{ywd} \cdot z \cdot \cot \theta) = 12.84 \text{ cm}^2/\text{m}$

6.2.3 (3): Eq. 6.8

$f_{ywd} = f_{yk} / \gamma_s = 435 \text{ MPa}$

Calculating the max. shear force $V_{Rd,max}$ in general that the concrete can bear $\rightarrow \cot \theta = \tan \theta = 1.0$.

$V_{Rd,max} = b_w \cdot z \cdot v_1 \cdot f_{cd} / (\cot \theta + \tan \theta)$

(NDP) 6.2.3 (3): Eq. 6.9

Maximum shear force $V_{Rd,max}$ occurs for $\theta = 45^\circ$: $\cot \theta = \tan \theta = 1$

$v_1 = 0.75 \cdot v_2 = 0.75$, $v_2 = 1$ for $\leq C50/60$

¹The tools used in the design process are based on steel stress-strain diagrams, as defined in [1] 3.2.7:(2), Fig. 3.8, which can be seen in Fig. 3.

²The sections mentioned in the margins refer to DIN EN 1992-1-1:2004 (German National Annex) [1], [2], unless otherwise specified.

$$V_{Rd,max} = 0.3 \cdot 0.384 \cdot 0.75 \cdot 17 / (1 + 1) = 734.4 \text{ kN}$$

Design with respect to EN 1992-1-1:2004 [3]:³6.2.3 (1): Inner lever arm z

$$z = 0.9 \cdot d$$

$$z = 0.9 \cdot 450 = 405 \text{ mm}$$

6.2.3 (2): Eq. 6.7N

The angle θ should be limited by Eq. 6.7N

$$1.0 \leq \cot \theta \leq 2.5 \rightarrow \cot \theta = 1.60 \text{ (choose for comparison)}$$

$$A_{sw,requ} / s = V_{Ed} / (f_{ywd} \cdot z \cdot \cot \theta) = 12.18 \text{ cm}^2/\text{m}$$

³The sections mentioned in the margins refer to EN 1992-1-1:2004 [3], unless otherwise specified.

5 Conclusion

This example shows the calculation of the required reinforcement for a rectangular cross-section under shear force. It has been shown that the results are reproduced with excellent accuracy.

6 Literature

- [1] *DIN EN 1992-1-1/NA: Eurocode 2: Design of concrete structures, Part 1-1/NA: General rules and rules for buildings - German version EN 1992-1-1:2005 (D), Nationaler Anhang Deutschland - Stand Februar 2010.* CEN. 2010.
 - [2] F. Fingerloos, J. Hegger, and K. Zilch. *DIN EN 1992-1-1 Bemessung und Konstruktion von Stahlbeton- und Spannbetontragwerken - Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau.* BVPI, DBV, ISB, VBI. Ernst & Sohn, Beuth, 2012.
 - [3] *EN 1992-1-1: Eurocode 2: Design of concrete structures, Part 1-1: General rules and rules for buildings.* CEN. 2004.
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