



Benchmark Example No. 11

Shear at the interface between concrete cast

SOFiSTiK | 2022

VERIFICATION DCE-EN11 Shear at the interface between concrete cast

VERiFiCATiON Manual, Service Pack 2022-12 Build 74

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The user of the program is solely responsible for the applications. We strongly encourage the user to test the correctness of all calculations at least by random sampling.



Overview

Design Code Family(s): DIN

Design Code(s): DIN EN 1992-1-1

Module(s): AQB

Input file(s): shear_interface.dat

1 Problem Description

The problem consists of a T-beam section, as shown in Fig. 1. The cs is designed for shear, the shear at the interface between concrete cast at different times is considered and the required reinforcement is determined.

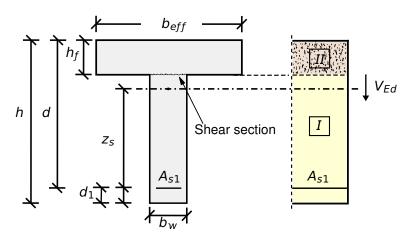


Figure 1: Problem Description

2 Reference Solution

This example is concerned with the shear design of T-sections, for the ultimate limit state. The content of this problem is covered by the following parts of DIN EN 1992-1-1:2004 [1]:

- Design stress-strain curves for concrete and reinforcement (Section 3.1.7, 3.2.3)
- Guidelines for shear design (Section 6.2)

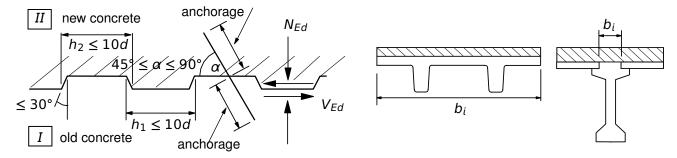


Figure 2: Indented Construction Joint - Examples of Interfaces

The design stress-strain diagram for reinforcing steel considered in this example, consists of an inclined top branch, as presented in Fig. 3 and as defined in DIN EN 1992-1-1:2004 [1] (Section 3.2.7).

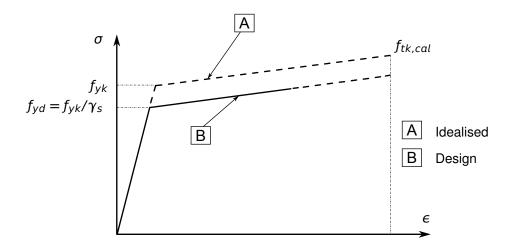


Figure 3: Idealised and Design Stress-Strain Diagram for Reinforcing Steel

3 Model and Results

The T-section, with properties as defined in Table 1, is to be designed for shear, with respect to DIN EN 1992-1-1:2004 (German National Annex) [1], [2]. The reference calculation steps [3] are presented in the next section and the results are given in Table 2.

Table 1: Model Properties

Material Properties	Geometric Properties	Loading
C 20/25	h = 135.0 cm	$V_Z = 800 \ kN$
B 500A	$h_f = 29cm$	$M_y = 2250 \ kNm$
	$d_1 = 7.0 \text{ cm}$	
	$b_w = 40 \ cm$, $b_{eff} = 250 \ cm$	
	$A_{s1} = 1.0 \ cm^2$	
	$z_s = 95.56 \ cm$	

Table 2: Results

a_s [cm ² /m]	SOF.	Ref.
state I	7.00	7.07
state II only V	4.86	4.90
state $II V + M$	4.99	4.99



Design Process 1 4

Design with respect to DIN EN 1992-1-1:2004 (NA) [1] [2]:²

Material:

Concrete: $\gamma_c = 1.50$

Steel: $\gamma_s = 1.15$

 $f_{ck} = 25 MPa$

 $f_{cd} = a_{cc} \cdot f_{ck}/\gamma_c = 0.85 \cdot 25/1.5 = 14.17 \text{ MPa}$

 $f_{vk} = 500 MPa$

 $f_{yd} = f_{yk}/\gamma_s = 500/1.15 = 434.78 MPa$

 $\sigma_{sd} = 456.52 \, MPa$

$$\tau = \frac{T_{v}}{b_{w}} = \frac{V \cdot S}{I_{v} \cdot b_{w}}$$

where S is the static moment of the separated area

$$S = h_w \cdot b_w \cdot (z_s - h_w/2) = 0.18058 \, m^3$$

$$\tau = \frac{0.8 \cdot 0.18058}{0.16667 \cdot 0.4} = 2.1669 MPa$$

$$T_{V} = \frac{0.8 \cdot 0.18058}{0.16667} = 0.86676 \, MN/m = 866.76 \, kN/m$$

$$T_{\rm V} = 866.76 / 2 = 433.38 \, kN/m$$

State *I*:

Design Load:

 $V_{Edi} = T_V = 433.38 \, kN/m$

 $v_{Edi} = \tau = 2.1669 \, MPa$

$$V_{Rd,c} = \left[C_{Rd,c} \cdot k \cdot (100 \cdot \rho_1 \cdot f_{ck})^{1/3} + 0.12 \cdot \sigma_{cp} \right] \cdot b_w \cdot d$$

$$v_{Rd,c} = C_{Rd,c} \cdot k \cdot (100 \cdot \rho_1 \cdot f_{ck})^{1/3} + 0.12 \cdot \sigma_{cp}$$

$$\rho_1 = \frac{A_{sl}}{b_w d} = 0.0 \rightarrow v_{Rd,c} = 0.0$$

with a minimum of

$$V_{Rd,c,min} = (v_{min} + 0.12 \cdot \sigma_{CD}) \cdot b_W \cdot d$$

 $v_{Rd,c,min} = v_{min} + 0.12 \cdot \sigma_{cp}$

$$v_{min} = (0.0375/\gamma_c) \cdot k^{3/2} \cdot f_{ck}^{1/2} = 0.20833 \text{ MPa}$$

defined in [1] 3.2.7:(2), Fig. 3.8, which can be seen in Fig. 3. ²The sections mentioned in the margins refer to DIN EN 1992-1-1:2004 (German Na-

tional Annex) [1], [2], unless otherwise specified.

¹The tools used in the design process are based on steel stress-strain diagrams, as

(NDP) 2.4.2.4: (1), Tab. 2.1DE: Partial factors for materials

Tab. 3.1: Strength for concrete

3.1.6: (1)P, Eq. (3.15): $a_{cc} = 0.85$ considering long term effects

3.2.2: (3)P: yield strength $f_{vk} = 500$

3.2.7: (2), Fig. 3.8

The shear section with a length of 0.4 m is split into two equal parts with b_i = $0.2 \, m$

The associated design shear flow V_{Edi}

(NDP) 6.2.2 (1): Eq. 6.2a: Design value for shear resistance $V_{Rd,C}$ for members not requiring design shear reinforcement

(NDP) 6.2.2 (1): Eq. 6.2b

(NDP) 6.2.2 (1): Eq. 6.3bDE



$$v_{Rd,c,min} = 0.20833 \rightarrow v_{Rd,c} = 0.20833 MPa$$

 $v_{Edi} > v_{Rd,c} \rightarrow$ shear reinforcement is required

6.2.5 (1): Eq. 6.23: The design shear stress at the interface should satisfy this $% \left(1\right) =\left(1\right) \left(1\right)$

(NDP) 6.2.5 (1): Eq. 6.25

Maximum shear stress $\nu_{Rdi,max}$ (NDP) 6.2.5 (1): $\nu=0.70$ for indented surface

6.2.5 (2): c, μ : factors depending on the roughness of the interface

(NDP) 3.1.6 (2)P: Eq. 3.16 $\alpha_{ct} = 0.85$

3.1.2 (3): Tab. 3.1 - Strength for concrete: $f_{ctk;0.05} = 1.8 \ MPa$:

 $\rho = \frac{a_{s}}{b_{l} \cdot l_{l}} \text{: area of reinforcement crossing interface / area of joint}$

 $V_{Edi} \leq V_{Rdi}$

$$v_{Rdi} = c \cdot f_{ctd} + \mu \cdot \sigma_n + \rho \cdot f_{vd} \cdot (1.2 \cdot \mu \cdot \sin \alpha + \cos \alpha)$$

and $v_{Rdi} \leq 0.5 \cdot v \cdot f_{cd}$

$$v_{Rdi,max} = 0.5 \cdot v \cdot f_{cd} = 4.9585 MPa$$

c = 0.50 and $\mu = 0.9$ for indented surface

$$f_{ctd} = \alpha_{ct} \cdot f_{ctk;0.05} / \gamma_c$$

$$f_{ctd} = 0.85 \cdot 1.80 / 1.5 = 1.02$$

$$v_{Rdi} = 0.5 \cdot 1.02 + 0 + \frac{a_s}{0.2 \cdot 1.0} \cdot 435 \cdot (1.2 \cdot 0.9 \cdot 1 + 0)$$

$$v_{Rdi} = 0.51 + \frac{a_s}{0.2} \cdot 469.56 = 2.1669$$

$$a_s = 7.07 \text{ cm}^2/\text{m}$$

State II only shear force V:

Design Load:

From the calculated inner lever arms for the two states we get a ratio:

$$\frac{z_I}{z_{II}} = 0.7664$$

The associated design shear flow V_{Edi} is:

$$V_{Edi} = 0.7664 \cdot 433.38 = 332.15 \, kN/m$$

and
$$v_{Edi} = 332.15/0.2 = 1.66 MPa$$

Following the same calculation steps as for state *II* we have:

$$v_{Rd,c} = 0.20833 MPa$$
 (as above)

 $v_{Edi} > v_{Rd,c} \rightarrow \text{shear reinforcement is required}$

 $v_{Edi} \le v_{Rdi}$

$$v_{Rdi} = c \cdot f_{ctd} + \mu \cdot \sigma_n + \rho \cdot f_{vd} \cdot (1.2 \cdot \mu \cdot \sin \alpha + \cos \alpha)$$

$$v_{Rdi} = 0.5 \cdot 1.02 + 0 + \frac{a_s}{0.2 \cdot 1.0} \cdot 435 \cdot (1.2 \cdot 0.9 \cdot 1 + 0)$$

$$v_{Rdi} = 0.51 + \frac{a_s}{0.2} \cdot 469.56 = 1.66$$

$$a_s = 4.90 \text{ cm}^2/\text{m}$$



State II shear force V and moment M:

$$M_{Eds} = 2250 \ kNm$$

$$\mu_{Eds} = \frac{M_{Eds}}{b_{eff} \cdot d^2 \cdot f_{cd}} = \frac{2250 \cdot 10^{-3}}{2.5 \cdot 1.28^2 \cdot 14.17} = 0.03876$$

$$\omega = 0.03971$$
 and $\xi = 0.9766$ (interpolated)

$$A_{s1} = \frac{1}{\sigma_{sd}} \cdot (\omega \cdot b \cdot d \cdot f_{cd} + N_{Ed}) = 39.44 \text{ cm}^2$$

$$z = \max\{d - c_{V,l} - 30 \text{ mm}; d - 2 c_{V,l}\}$$

$$z = \max\{1160; 1190\} = 1190 mm$$

Design Load:

$$T_V = V / z = 800 / 1.19 = 672.268 \, kN/m$$

$$T_V = 672.268 / 2 = 336.134 \, kN/m$$

$$V_{Edi} = 336.134 \, kN/m$$

and
$$v_{Edi} = 336.134 / 0.2 = 1.68 MPa$$

$$v_{Rd,c} = C_{Rd,c} \cdot k \cdot (100 \cdot \rho_1 \cdot f_{ck})^{1/3} + 0.12 \cdot \sigma_{cp}$$

$$C_{Rd,c} = 0.15/\gamma_c = 0.1$$

$$k = 1 + \sqrt{\frac{200}{d}} = 1 + \sqrt{\frac{200}{1280}} = 1.3953 < 2.0$$

$$\rho_1 = \frac{A_{sl}}{b_w d} = \frac{39.44}{40 \cdot 128} = 0.007703 < 0.02$$

$$v_{Rd,c} = 0.1 \cdot 1.3953 \cdot (100 \cdot 0.007703 \cdot 25)^{1/3} + 0$$

$$v_{Rd,c} = 0.373229 MPa$$

 $v_{Edi} > v_{Rd,c} \rightarrow$ shear reinforcement is required

$$v_{Rdi} = c \cdot f_{ctd} + \mu \cdot \sigma_n + \rho \cdot f_{vd} \cdot (1.2 \cdot \mu \cdot \sin \alpha + \cos \alpha)$$

$$v_{Rdi} = 0.5 \cdot 1.02 + 0 + \frac{a_s}{0.2 \cdot 1.0} \cdot 435 \cdot (1.2 \cdot 0.9 \cdot 1 + 0)$$

$$v_{Rdi} = 0.51 + \frac{a_s}{0.2} \cdot 469.56 = 1.68$$

$$a_s = 4.99 \text{ cm}^2/\text{m}$$

Tab. 9.2 [4]: ω —Table for up to C50/60 without compression reinforcement

$$N_{Ed}=0$$

(NDP) 6.2.3 (1): Inner lever arm z

The shear section with a length of 0.4 m is split into two equal parts with $b_i = 0.2 m$

(NDP) 6.2.2 (1): $C_{Rd,c} = 0.15/\gamma_c$



5 Conclusion

This example shows the calculation of the required reinforcement for a T-section under shear at the interface between concrete cast at different times. It has been shown that the results are reproduced with excellent accuracy. Small deviations occur because AQUA calculates (by using FEM analysis) the shear stresses more accurate compared to the reference example.

6 Literature

- [1] DIN EN 1992-1-1/NA: Eurocode 2: Design of concrete structures, Part 1-1/NA: General rules and rules for buildings German version EN 1992-1-1:2005 (D), Nationaler Anhang Deutschland Stand Februar 2010. CEN. 2010.
- [2] F. Fingerloos, J. Hegger, and K. Zilch. *DIN EN 1992-1-1 Bemessung und Konstruktion von Stahlbeton- und Spannbetontragwerken Teil 1-1: Allgemeine Bemessungsregeln und Regeln für den Hochbau.* BVPI, DBV, ISB, VBI. Ernst & Sohn, Beuth, 2012.
- [3] Beispiele zur Bemessung nach Eurocode 2 Band 1: Hochbau. Ernst & Sohn. Deutschen Betonund Bautechnik-Verein E.V. 2011.
- [4] K. Holschemacher, T. Müller, and F. Lobisch. *Bemessungshilfsmittel für Betonbauteile nach Eurocode 2 Bauingenieure*. 3rd. Ernst & Sohn, 2012.