



Benchmark Example No. 1

## Joint Deflection of Plane Truss

SOFiSTiK | 2022

**VERiFiCATION**  
**BE1 Joint Deflection of Plane Truss**

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The manual and the program have been thoroughly checked for errors. However, SOFiSTiK does not claim that either one is completely error free. Errors and omissions are corrected as soon as they are detected.

The user of the program is solely responsible for the applications. We strongly encourage the user to test the correctness of all calculations at least by random sampling.

**Front Cover**

Arnulfsteg, Munich Photo: Hans Gössing

Overview	
<b>Element Type(s):</b>	TRUS
<b>Analysis Type(s):</b>	STAT
<b>Procedure(s):</b>	
<b>Topic(s):</b>	
<b>Module(s):</b>	ASE
<b>Input file(s):</b>	truss.dat

## 1 Problem Description

The problem consists of a plane truss structure, as shown in Fig. 1. Determine the vertical deflection at the free node 8.

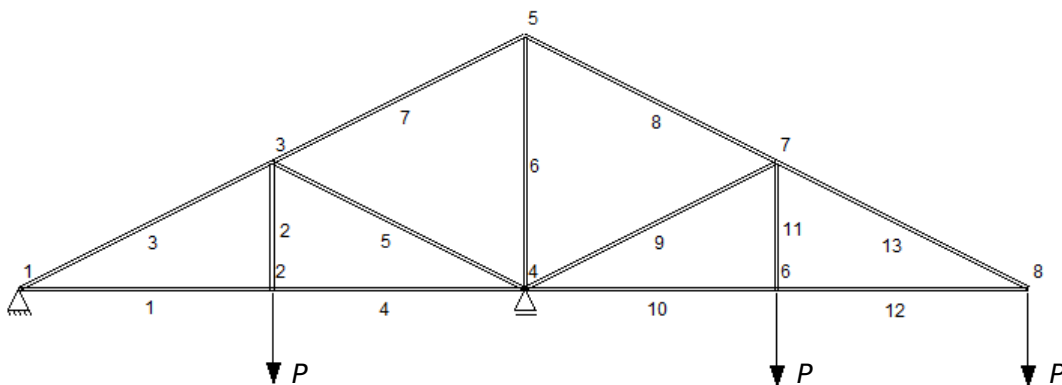


Figure 1: Problem Description

## 2 Reference Solution

The problem of determining the displacements of trusses can be treated in various ways. Popular among engineers, is to apply energy methods, e.g. the method of virtual work or Castigliano's theorem, to solve problems involving slope and deflection, that are based on the conservation of energy principle, and are more suitable for structures with complicated geometry such as trusses. Further information on this topic can be found in numerous engineering books, dealing with structural analysis [1].

## 3 Model and Results

The general properties of the model [2] are defined in Table 1. The total width of the truss is 60 ft, consisting of four spaces of 15 ft each, and the total height is 15 ft. The load is applied equally at the three free nodes at the bottom of the truss. The results are presented in Table 2 and compared to the reference example [2]. Fig. 2 shows the deflections and the deformed shape of the structure.

Table 1: Model Properties

Material Properties	Geometric Properties	Loading
$E = 29 \cdot 10^3 \text{ ksi}$	$l_{total} = 60 \text{ ft} = 18.288 \text{ m}$	$P = 20 \text{ kip} = 89.0 \text{ kN}$
$= 206842.773 \text{ MPa}$	$h_{total} = 15 \text{ ft} = 4.572 \text{ m}$	

Table 1: (continued)

Material Properties	Geometric Properties	Loading
$\nu = 0.3$	$l_2 = l_{11} = 7.5 \text{ ft} = 2.286 \text{ m}$ $l_1 = l_4 = l_6 = l_{10} = l_{12} = 15 \text{ ft} = 4.572 \text{ m}$ $A_1 = A_4 = 2 \text{ in}^2 = 12.90 \text{ cm}^2$ $A_2 = A_{11} = A_{10} = A_{12} = 1 \text{ in}^2 = 6.45 \text{ cm}^2$ $A_5 = A_9 = 1.5 \text{ in}^2 = 9.68 \text{ cm}^2$ $A_3 = A_6 = 3 \text{ in}^2 = 19.35 \text{ cm}^2$ $A_7 = A_8 = 4 \text{ in}^2 = 25.81 \text{ cm}^2$	

Table 2: Results

	SOF.	Ref. [2]	$ e_r $ [%]
$\delta_8$ [mm]	69.11	69.09	0.036

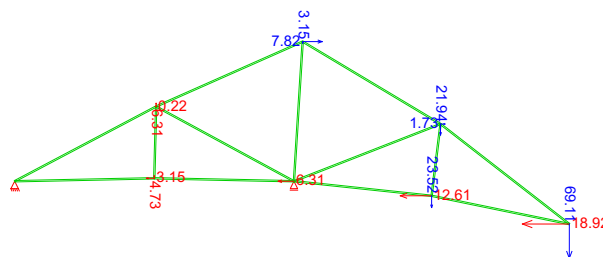


Figure 2: Problem Description

## 4 Conclusion

This example verifies the deflection of trusses. It has been shown that the behaviour of the truss is accurately captured. It should be noted that in the reference example [2] the deflection in inches was rounded to two decimal places, which leads to a higher relative error in Table 2. When comparing the SOFiSTIK result with an analytical solution rounded to four decimal places, the relative error decreases to 0.0004%.

## 5 Literature

- [1] R. C. Hibbeler. *Structural Analysis*. 8th. Prentice Hall, 2012.
- [2] J. C. McCormac. *Structural Analysis*. Wileys & Sons, 2007.